



Advances and Applications of Rapid Electrokinetic Patterning

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Abstract | The dynamic manipulation and assembly of colloids enables the advancement of analytical techniques in biotechnology and the development of self-assembled materials. Rapid electrokinetic patterning (REP) is a hybrid optoelectrokinetic technique that simultaneously uses a laser illumination and a uniform AC electric field to yield programmable, dynamic, and non-invasive manipulation of colloidal particles. Since it was introduced, the technique has been applied to microengineering and biological research fields, showing its promising capabilities as a great tool for trapping, aggregating, translating, and sorting single and multiple micro- and nanoparticles, including bacteria. To effectively leverage and enhance these applications, this review paper will highlight its versatility and capability, including REP's principles, governing physics, different experimental setups, fabrications, applications, and future prospects.

1 Introduction

The need to control micro and nanoparticles are essential in microfluidic platforms involving in vitro biological applications or general micro- and nanoparticle colloidal manipulation. Current manipulation techniques that offer a label-free control and manipulate such entities include active systems such as dielectrophoresis,², ^{27, 30, 37, 50, 54, 56} electrophoresis,^{17, 31, 45, 82} optical trapping,^{3, 11, 22, 86} acoustophoresis,^{16, 40, 54, 64, 71} and hydrodynamic forces.^{8, 19, 66, 69, 85} These techniques require an external stimulus that interacts with the intrinsic properties of the bio-particles including their dielectric properties, optical properties, morphology, and/or chemical state. Labelbased techniques like magnetophoresis^{1, 15, 55, 57,} ^{62, 68} require extra labeling. Although these techniques revolutionized the biotechnology field with their capability of trapping,^{13, 53} concentrat-ing,⁷² focusing,^{9, 87} sorting,^{7, 26, 56} separating,^{4, 42, 84} detecting,⁶⁷ counting, lysing, and filtering²⁵ bioparticles, they either lack high resolution^{5, 12, 41} or high throughput manipulation.^{5,65}

Bio-particles manipulated using aforementioned active label-free electrokinetic techniques require the application of a proper electric field to avoid unwanted electrokinetic effects. For example, a large electric field will harm the viability and growth of the cells being analyzed^{43, 87} and is exacerbated when DC voltages or high voltages at lower frequencies are applied.²⁸ Another unfavorable factor that limits the application of higher electric fields is Joule heating which causes the local temperature of the medium to rise in response to the applied field. Joule heating is also responsible for the formation of bubbles inside the microchannels which compromise device performance. Jaeger et al. found that the electric field induced temperature rise is linearly proportional to increasing the electric conductivity of the medium. However, most of biological cells require suspension in high electric conductive media (>0.1 S m⁻¹). Hence, reducing buffer conductivity is required to suppress the Joule heating. High electric fields are required to enhance the range of dielectrophoretic force which decays far from planar electrodes. 3D electrode design can

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KEVI. \RTIC help to minimize dielectrophoretic force decay,⁴⁴ which will minimize the Joule heating 8–10 times lower than in planar electrode designs.⁷⁰ However, such design will add an additional fabrication cost and complexity. Hence, the current trend is to develop new electrokinetic techniques that use new fabrication methods or integrate additional physical mechanisms to synergistically achieve a wide range of resolution, high throughput, and robust non-invasive manipulation.

REP is a technique that merges the advantages of high resolution, dynamic manipulation of optical tweezers with the high throughput of AC electrokinetics resulting in precise, dynamic, and programmable control of colloids.^{32, 79, 80} REP uses a parallel plate electrode system that provides AC electrokinetic forces and a highly focused laser beam that induces localized 'hot-spots' on the electrodes. Electrothermal flows are generated due to the sharp thermal gradients induced by the localized hot-spots. The application of the electric field acting upon these gradients, result in electrothermal hydrodynamic motion that carries the suspended particles towards the trapping region, achieving rapid accumulation and patterning at a desired location on the electrode surface. A variety of particles have been manipulated by Williams et al. using different schemes of optical landscapes (Fig. 1).⁷⁶ When both the laser irradiation and electric fields are applied, particles can be concentrated rapidly within the irradiated spot (Fig. 1b), the size of cluster can be modulated by either increasing the size of the irradiated spot or the intensity of laser illumination. Not only can REP trap and concentrate micro- and nanoparticles but it can also translate and concentrate them at any desired spot on the electrode (Fig. 1c, g, i).

REP colloidal accumulation is frequency dependent, enabling selective concentration of particles as well as sorting (Fig. 1f).⁷⁸ In the low frequency regime (<200 kHz) Williams et al. successfully trapped and dynamically patterned micrometer particles on an indium tin oxide (ITO) electrode surface by utilizing various optical schemes produced from a laser operating at a wavelength of 1064 nm. REP is a versatile technique and particles as diverse as silica particles⁸¹ and polystyrene particles⁸⁰ (50 nm-3 µm) have been successfully assembled. REP offers significant benefits to lab-on-a-chip (LOC) systems devised for biological or chemical analysis. Conducting high accurate analysis and throughput by implementing REP will improve the performance of biochemical sensors, diagnostic biochemical devices for biological assays,38,76 enhanced detection for diabetic retinopathy,⁷⁵ as well as trapping and deposition of multiwalled carbon nanotubes. $^{47}\,$

REP is a novel technique with high potential and capabilities to be integrated to enhance various biological, biotechnological and lab-on-a-chip fields. This review article will: (1) highlight the efforts done by researchers to provide physical understanding of REP through experimentation and modelling as well as characterizing its electrokinetic mechanisms, (2) summarize the initial experiments and results of REP showcasing its potential, and attempted applications, and (3) discuss current challenges, future opportunities, and alternative inexpensive REP platforms.

2 REP Setup and Operation

In a REP chip, two conductive ITO-coated transparent glass plates are separated by a suitable spacer (50–100 μ m) such as a commercial double side adhesive tape patterned with a razor or laser cutter. Inlet and outlet reservoirs were achieved by drilling through the (Fig. 2a)^{33, 76, 79, 80} ITOcoated transparent glass substrates which were used in parallel with different metal-coated glass plates, in both cases the laser irradiated spot was applied on either plate. However, as ITO has a high electrical resistance, other more conductive metals such as copper, gold, and a chromecoated electrode also may be used (Table 1). The chosen conductor needs to absorb sufficient illumination to induce electrothermal flow, applications of REP have primarily used ITO with NIR (1064 nm) illumination (Fig. 2b)^{33, 35, 75–77, 79, 80} the media itself does not directly absorb significant laser illumination.

The optically induced temperature gradient generates gradients of conductivity and permittivity that coupled with the applied AC electric field creates a toroidal electrothermal vortex (Fig. 2a). A crucial parameter to consider in the experimental setup is optical skin depth of the electrode material being used; each material has an optimal thickness that can achieve highest absorption of the laser irradiation, for ITO material this thickness is approximately 700 nm with an absorption coefficient of 1.3×10^5 m^{-1,29} which is greater than the typical ITO thickness commercially available (350 nm). Nickel, with its higher absorption coefficient than ITO $(5.59 \times 10^7 \text{ m}^{-1})$ and optical skin depth of 17.9 nm, has been tested and showed 2.4×10^4 K W⁻¹ (Kelvin per laser power) while titanium was found to be 3.5×10^4 K W⁻¹ with an optical skin depth of 21.06 nm.^{29, 48} At the same laser power, titanium will absorb laser



Figure 1: Particles manipulated with REP: **a** no trapping of particles in the initial state, **b** aggregation of 5 µm particles at 5 kHz, **c** translation of 5 µm trapped particles at 5 kHz, **d** single particle manipulation (5 µm) at 17 kHz, **e** simultaneous trapping of 1 and 5 µm particles at 5 kHz, **f** 1 µm particles sorted by size at 36 kHz, **g** L-shaped patterning of 5 µm particles, **h** single particle patterning (5 µm particles), and **i** 22 nm particle aggregation at 5 kHz and 16.5 V_{pp}. Reproduced with permission of the Royal Society of Chemistry



Figure 2: a Illustration of REP operation. b Schematic of the experimental setup. c Microchannel formation sandwiched between the parallel ITO electrodes. a, b Reproduced with permission of the Royal Society of Chemistry.²⁰ c⁻¹.

Table 1: Reported REP e>	perimental conditions.		
AC frequency	1–200 kHz		
Applied electric field	$6 \times 10^4 5 \times 10^5 \ V_{pp} \ m^{-1}$		
Diameter of manipulated particles	0.05–3 μm		
Buffer conductivity	$< 150 \text{ mS m}^{-1}$		
Heating method	Laser illumination $\lambda = 532$ nm	Gold-coated electrodes (6.4–150 nm thick)	
	Laser illumination $\lambda = 1064$ nm	ITO coated electrodes (0.7 µm thick)	20–30 mW
			Max temperature increase < 10 °C
	Resistive heating	Copper/gold	Max temperature increase 18 °C and gradient 0.5 °C μm^{-1} with 1.6 V_{pp}

irradiation higher than nickel or ITO, hence it will generate higher thermal gradients which will generate greater electrothermal flow. Therefore, an expensive high-power laser source may be replaced with inexpensive optical source to generate the illumination required to induce the thermal gradient.^{29, 48, 78} This feature is crucial as it allows REP to conduct at different optical wavelengths, provided that a proper combination of laser power, wavelength, and electrode material is chosen to generate the necessary optically induced temperature gradients.^{35, 48, 78}

The programmable laser source in REP dynamic operation is typically applied using a hologram generated from a spatial light modulator or scanning laser system,⁷⁴ being focused by a high numerical aperture objective lens. Low conductivity buffers were used, typically deionized water^{33, 34, 38, 78–80} conductivities up to 150 mS m⁻¹ has been attempted though are not seemingly viable as some of the governing electrokinetic mechanisms are suppressed at elevated conductivities (see next section). Further, in the case of using a high conductivity electrolyte (σ >200 mS m⁻¹), Joule heating will need to be monitored. However, it is important that future REP platforms be applied towards moderate $(\sim 100 \text{ mS m}^{-1})$ or high conductivity media to handle an assortment of biological cells.

3 Physical Mechanisms of REP

As REP operation is a hybrid opto-electrokinetic mechanism, it requires a simultaneous application of a uniform AC electric field as well as laser illumination. REP particle trapping is achieved by a precise balance of several electrokinetic forces. First, bulk electrothermal flow is generated at the center of the illumination. The laser induces nonuniform thermal gradients in the medium causing local changes in fluid conductivity and permittivity which respond to the applied field. Natural convective flow is generally negligible for this microfluidic system.^{24, 30, 31, 39, 81} Second, particle-induced AC electroosmosis (ACEO) is an electrohydrodynamic (EHD) mechanism that influences particle–electrode and particle–particle interactions.^{34, 78, 81} Thanks to the synergetic effect between these two mechanisms trapping and patterning is possible using REP.

The time-averaged expression for this electrothermal body force is²⁰

$$\langle F_{e} \rangle = \frac{1}{2} \operatorname{Re} \left(\frac{\sigma \varepsilon (\alpha - \beta)}{\sigma + i\omega \varepsilon} (\nabla T \cdot E) E^{*} - \frac{1}{2} \varepsilon \sigma |E|^{2} \nabla T \right),$$
(1)

where Re() refers the real part of the expression, E is the electric field, E^* is its complex conjugate, T is the temperature, ω is the applied frequency, σ is the conductivity of the fluid, ε is the permittivity of the fluid, β is $(1/\sigma)(\delta\sigma/\delta T)$ and a is $(1/\varepsilon)(\delta\varepsilon/\delta T)$. The first and second term in (1) is the Coulomb force and the dielectric force, respectively; the first term will dominate until the frequency exceeds the charge relaxation of the fluid. Each term is dependent on the magnitude of the temperature gradients (∇T) which can be generated through Joule heating²⁰ or illumination.^{21, 36, 49} The latter drives fluid motion within REP and, further, bulk Joule heating is neglected since the fluid conductivity is low and the applied field is uniform; therefore, the electrothermal body force scales as the second power of the electric field $(|E|^2)$.^{60, 78} One special case of REP

heating has the source of non-uniform heat from micro-patterned DC heaters.⁷³

There exist a variety of frequency-dependent electrokinetic and electrohydrodynamic interactions in REP. These forces are grouped into four types (Fig. 3a)⁷⁶: (1) particle-electrode attraction force, F_{e} , (2) dipole-dipole repulsion force, F_{r} (3) drag force induced from the electrothermal flow (lateral, F_a and vertical, F_d), and (4) particle–particle EHD attraction, F_a .^{52, 61} All of these electrokinetic forces are a function of AC frequency; therefore, a proper frequency needs to be chosen to balance these forces.⁸¹ This is because at lower frequencies F_d is constant and it helps to drag the particles near the electrodes surface. Next, F_e results in trapping particles on the electrode surface where their crystallinity, aggregation and spacing is governed by F_a . As frequency increases, F_a weakens and the dipoledipole resistive force, (F_r) increases interparticle spacing until the frequency reaches the particle's critical frequency at which time it is released from the electrode surface. Aggregation characteristics are a function of the particle size, particle surface charge, and the applied field amplitude and frequency. At high frequencies (>1 kHz) a low-density phase was observed while at low frequencies compact disconnected particle aggregations occurred. At higher frequencies particles are swept away from the accumulated cluster by the electrothermal flow force due to the relaxation of particle-electrode forces. There is a critical frequency for maintaining REP aggregations and is related to the polarization of the particles' electrical double layer.^{33, 52, 78} Therefore, REP can be used to trap and sort particles based on their frequency-dependent double-layer polarization

behavior. Once the applied frequency approaches the critical frequency the particle cluster becomes unstable and is swept away by electrothermal flow. A particle's critical frequency decreases with increasing particle size (Fig. 3b), specifically the particle–electrode force has an inverse dependence on the surface area of the particle. This critical frequency is key factor for separating or sorting colloidal particles applications.

Williams et al.⁸¹ demonstrated the separation of 1 μ m from 2 μ m spheres by retaining the smaller particles at lower frequencies. Kwon et al.³⁸ performed separation of *Staphylococcus aureus* (*S. aureus*) bacterium (~1 μ m in diameter) from *Saccharomyces cerevisiae* (*S. cerevisiae*) (~5 μ m in diameter) based on their sizes.

Table 2 summarizes the main REP electrokinetic mechanisms with their underlying physics including their dependence on frequency. The electrohydrodynamic mechanism leading to compact particle aggregations is derived from field perturbations caused by the interaction between the polarized particle and electrode. The induced imbalance of charge on the electrode polarization layer causes local EHD. Ristenpart et al.⁶¹ predicted that these electrohydrodynamic forces scaled with the square of the electric field strength (E^2) and the inverse of frequency (ω^{-1}). The dipole-dipole repulsive force is an additional particle-particle interaction that scales with the square of the electric field (E^2) and to the sixth power of the particle radius (a^6) . This relationship provides a good estimation of particle forces for applied AC frequencies greater than 500 Hz.¹⁴ Within REP, the dipole-dipole repulsive force becomes dominant at higher frequencies as particle-electrode EHD are suppressed.





Table 2: REP mechanisms with t	their underlying physics, scaling, and range	of frequency dependence.		
Mechanism	Observed behavior	Physics	Scaling	Cita- tion
Electrothermal fluid motion (F _D)	Inward fluid vortices generated at the center of the focused laser Transports particles near the electrode surface Lateral drag to compact trapped particles	Local change in permittivity and conductivity induced by laser Gradients in dielectric properties combined with the electric field induce fluid motion First term in (1) is dependent on frequency, the second term is negligible in REP	Effectively, fluid motion is constant at low frequencies with; $F_D \propto \text{heating power} (\sim \nabla T)$ $F_D \propto E^2$ $F_D \text{ is independent on particle size or type Until the fluid's charge relaxation is met (\omega > 5 \text{ MHz}), then decreases and becomenegligible$	6, 78
Particle-electrode electrokinetics ($F_{\rm E}$)	Takes place at low frequencies and results trap- ping particles on the electrode surface	Particle-induced field gradients near the elec- trode surface induce localized EHD	Critical frequency above which particles cannot be held in the REP trap $\omega_c \propto 1/p$ article surface area (a^2) $F_E \propto E^2$ T/d (distance from electrode)	14, 60, 81
Particle–particle electrokinetics	Frequency governs crystallinity of the aggrega- tion	Controlled by attractive particle-induced EHD (F_a) and repulsive dipole–dipole forces (F_r) .	$F_a, F_r \propto E^2$ At low frequencies: F_a is governed by local EHD flow and particles aggregate At high frequencies: EHD is suppressed and F_r is dominant; $F_r \propto a^6$ $F_r \propto 1/\sigma$	60, 78

Williams⁷⁸ studied REP particle–particle interactions and investigated its influence on inter-particle distance within aggregations.⁸³ They also established that there exists a frequency where a minimum distance is observed for different particles size. They also observed that the particles on the perimeter of the aggregation were spaced further apart from their neighbors due to the weaker hydrodynamic drag they experienced further from the vortex's center. They also revealed that particle–particle distance was independent of voltage since the aforementioned electrokinetic mechanisms (ACEO, electrothermal hydrodynamics, dipole–dipole repulsive forces) scale with the square of the applied electric field.

By altering the AC frequency, a myriad of particle-particle electrokinetic interactions can be achieved, particularly for solutions with different particle sizes. When the particle-particle distance reaches its minimum value, compact structures resulted in a semi-stable aggregate that held firmly to the electrode surface, resisting further hydrodynamic drag from the microfluidic vortex. Smaller particle aggregations tend to form multiple layers⁸⁰ whereas particles greater than 1.0 µm in diameter remain arranged as a monolayer aggregation.⁷⁸ The role of particle diameter and surface chemistry need to be investigated further to enable the creation of precisely tuned artificial architectures such as reconfigurable colloidal crystals. For example, since dipole-dipole forces scale with a^6 , even larger particles (~10 µm) can form chains in the direction of the field (aka "pearl chaining"^{10, 58, 59} while their assembly can be guided by bulk electrothermal flow, resulting in the generation of 3D assembled structures.

Work and Williams⁸³ investigated the particle-to-particle spacing for an REP aggregation as a function of laser-scanning length. They found that the average particle-particle spacing has a linear relationship with the length of the scanning laser. As long as the heating induced optically is evenly distributed across the scanned line, that linear relationship should be valid, maintaining a steady microfluidic vortex profile. Thus, upon decreasing the induced temperature gradients, particles become more spaced apart at increasing scan lengths due to the resultant decreased hydrodynamic drag. Additional information on REP mechanisms, including the critical frequency, patterning and crystallinity are available in previous publications. 33-36, 74, 78, 79, 80, 83

4 REP Applications

The promising abilities of REP have been shown in different applications including the aggregation, translation, sorting, and patterning of single and multiple artificial micro and nanoparticles, as well as, viable particles such as bacteria. The following will provide an overview (Table S1) of the published material on the use of REP in these diverse applications.

4.1 General Patterning/Shape Modulation

For most initial REP demonstrations, the optical light source consisted of a focused light beam, where particles were arranged within a circular spot (Fig. 1b). However, patterning particles into more complex geometries is also possible^{73, 79} and applicable in investigations of artificial structures involving colloidal crystalline assemblies. One REP example utilizes the conventional parallel plate ITO chip (Fig. S1), and an illumination source consisting of a near infrared holographic system. The shapes of the holographic optical landscapes were controlled by computer-programmed spatial light modulators that modified and replicated different light patterns. As a demonstration, Williams et al. showed a polystyrene (690 nm) particle assembly in the shape of an "L" (Fig. 4a, b).⁷⁹ In these experiments, REP was carried out with an AC signal of 2.0 V_{pp} at 1.6 kHz and an illumination intensity of 20 mW. By increasing the illumination intensity and voltage, larger trapping regions and particle aggregations were generated. Though the example only portrays polystyrene particles, similar observations were seen for latex and silica particles ranging from 300 nm to 3 µm.

Complex geometries of particle aggregations have also been achieved using a modified REP chip, containing thin film heaters (Fig. 4c-f).⁷³ The benefits of the thin film REP devices include its cost-effective thermal efficiency, simple/scalable fabrication, potential for higher throughput, and ability to integrate with other microsystems. In this modified REP chip, arrays of micropatterned thin films of copper were embedded within a glass substrate. The copper thin films are used as DC controlled heaters to create highly non-uniform temperature fields. Particles were assembled in the shape of the heater geometry, either a line (Fig. 4c, d) or "X" (Fig. 4e, f) wire trace at 10 V_{pp} and 100 kHz with 1.6 V_{DC} applied to the heaters. The thin film heaters make it possible to have several simultaneous trapping areas within a single platform. Initially, a single layer of particles $(1 \ \mu m)$ were assembled. As the number



Figure 4: Depictions of complex geometries formed with REP: **a** optical landscape and **b** respective polystyrene particle (690 nm) assembly in the shape of an "L" with an AC signal of 2.0 V_{pp} at 1.6 kHz and an illumination intensity of 20 mW. Reproduced with permission of the Royal Society of Chemistry. **c** Schematic of REP thin film heater device during particle aggregation. Particles were shown to assemble in the shape of the heater geometry. **d** For the line heaters, 1.0 µm particles were trapped at 1.6 V_{DC}, 10 V_{pp}, and 100 kHz. **e**, **f** Devices with "X" heaters accumulated particles at 1.6 V_{DC}, 10 V_{pp}, and 110 kHz. Reproduced with permission of Elsevier".

of particles trapped increased, a second and third layer of particles were collected, forming triangular tetrahedrons due to decreased drag and attractive dipole–dipole interactions.

REP can also be used to trap a particle cluster near the electrode surface in the simultaneous presence of bulk fluid flow.⁷⁹ Using the holographic optical illumination system and parallel electrode ITO platform, latex particles (1 μ m) were assembled on the electrode surface at an AC signal of 10 V_{pp} at 5 kHz, illumination intensity of 40 mW, and pressure driven bulk fluid flow at 120 μ m s⁻¹. The combination of REP and bulk microchannel flow will result in a concentrated stream of microparticles along the electrode surface. This ability has potential benefits in improving the performance of sensor-based lab-on chip systems, where the sensors are located along the surface of the microchannel.

Despite the dynamic benefit of REP that allows for particle clusters to be reconfigured into various shapes and translated to new areas in the electrode surface, these aggregations will disperse with the deactivation of the applied illumination pattern or AC field. However, particle assemblies can be permanently adhered to the electrode surface through the brief application of a DC offset voltage of 2.5 V.^{23, 47, 79} It has been postulated that this phenomena results from electrophoretic forces manipulating the particles close to the substrate such that van der Waals forces permanently immobilize particles onto the substrate.¹⁸ This ability to permanently pattern particles onto the electrode surface enables REP to be useful in area of colloidal assembly for micro and nano-manufacturing.

4.1.1 Patterning Nanoparticles

REP also has the ability to aggregate nanoparticles (Figs. 1i, 5). Unlike optical trapping techniques which are limited by Brownian motion and weak optical trapping forces, REP has been shown to concentrate and assemble polystyrene particles with diameters of 49–100 nm⁷⁸ as well as gold and silver nanoparticles with diameters of 40–200 nm.⁴⁷ The details on the constitution of the REP chip and experimental setup can be found in Williams.⁷⁸ For nanoparticle aggregation, an illumination intensity of 0.18 W and an AC signal of 14 V_{pp} at 10 kHz trapped 100 nm particles in a single spot on the gold electrode





surface (Fig. 5a). An illumination intensity of 0.18 W and an AC signal of 14 V_{pp} at 10 kHz trapped 100 nm particles in a single spot on the gold electrode surface (Fig. 5a). Implementing the spatial light modulators, the 100 nm particles were captured in three spots at an increased laser power of 0.4 W (where only 15% of this reached the sample) (Fig. 5b). It must be noted that for nanopatterning REP application, highly smooth surfaces are required to minimize any roughness or imperfection (that is in the order of or greater than the particle size) to deter any localized, non-uniform electrokinetics.

4.1.2 Patterning Bacteria

Most of REP applications discussed so far has focused on the trapping and manipulation of artificial colloids. However, some biological applications were also explored. REP has been shown to trap and manipulate swimming bacteria (*Enterobacter aerogenes*, Fig. 6a–e).⁴⁸ In this study,

the effects of REP conditions such as the optical radiation and laser induced heating (applied for 4 min) have only shown to indicate insignificant effects on cell viability. It was shown that only high electric fields of 200 k V_{pp} m⁻¹ for 5 min caused electroporation in 21% of cell population. REP effectively traps bacteria swimming at average speeds of 23 μ m s⁻¹ within a parallel ITO electrode chip and fluidic chamber 100 µm in height. At the application of an AC electric field, bacteria (107 cells mL-1) suspended in diluted PBS were affected by electro-orientation^{46, 51}, which results in the polarization and thus an induced dipole along one axis, where the reorientation is in the vertical direction (direction of electric field) of 98% of the bacteria population. At AC signal of 110 kV_{pp} m⁻¹, 20 kHz, and 20 mW, bacteria were swept by the electrothermal vortex to the stagnation and held there by particle-electrode interactions.

Additionally, REP was used to aggregate and handle various species of bacteria, including



Figure 6: REP used to trap and sort bacteria. **a** *Enterobacter aerogenes* were trapped and translated on an ITO electrode surface at the onset of an electric field of 110 kV_{pp} m⁻¹, 20 kHz, and laser power of 20 mW. Images were acquired for **b** motile *E. aerogenes* before and after **c** the application of electric field. The electric field generated a torque on the bacteria and rotating them vertically, parallel to the direction of the field. **d** Once the laser spot was illuminated on the electrode surface, *E. aerogenes* were accumulated. **e** *Enterobacter aerogenes* lose their vertical orientation and were released once both the AC signal and laser spot were turned off. Reproduced with permission of the Royal Society of Chemistry⁻¹.

Shewanella oneidensis (S. oneidensis) MR-1, Saccharomyces cerevisiae (S. cerevisiae), and Staphylococcus aureus (S. aureus).³⁸. For this study, the established experimental setup consisting of the parallel plate ITO chip and Nd: YVO4 laser (1064 nm wavelength) were used. The motile, rod-shaped bacteria S. oneidensis MR-1 (~1 µm in diameter and 2-3 µm length) were shown to accumulate at an AC signal of 17.8 V_{pp} and 18.7 kHz and a laser of power of 20 mW. The onset of the electric field and laser beam caused over 700 bacteria to align in the vertical direction and be dragged towards the illumination spot by the toroidal microvortex within 0.73 s. Multiple aggregations of bacteria in the same substrate were also formed through two focused laser spots on the substrate. Authors observed that after disabling the AC field and laser spot, bacteria were motile and assumed unharmed by REP effects.

4.1.3 Patterning MWCNTs

REP has the ability to collect and manipulate a single to 100 vertically aligned multi-walled carbon nanotubes (MWCNT) (Fig. 7).⁴⁷ The experimental details can be referenced in Mishra

et al.47 publication. Experiments were carried out at 20 mW, with AC electric fields and frequencies between 100–140 $kV_{pp}\ m^{-1}$ and 10–100 kHz, respectively. Single MWCNTs in deionized water solution $(1.3 \times 10^7 \text{ CNTs mL}^{-1})$, 0.37 ± 0.04 mS m⁻¹) were captured and manipulated with a 20 mW laser beam and an AC signal of 140 kV_{pp} m⁻¹ and 55 kHz (Fig. 7g–j). The applied electric field produced a dipole moment on the nanotube and generated a torque that flipped the nanotube in the vertical direction, parallel to the electric field. The aggregation of several vertically aligned-MWCNTs was accomplished with a MWCNT solution of 1.6×10^8 CNTs mL⁻¹ (0.37 ± 0.04 mS m⁻¹), 20 mW laser beam, and AC field of 140 $kV_{_{\rm DD}}\,m^{-1}$ at 15 kHz (Fig. 7a-f). Similarly, these nanotubes experienced a torque that aligned them in the direction of the field, while the electrothermal vortex overcome dipole-dipole repulsive forces that increase the separation between the nanotubes.³⁵ The authors observed that removing the illumination increases the distance between the MWCNTs, while the removal of the electric field causes the MWCNTs to lose their vertical orientation.



Figure 7: Depictions of **a**-**f** multiple and **g**-**j** single trapped MWCNTs within a REP platform. Diagrams and images of several **a** free MWCNTs and **b**, **e** captured vertically aligned MWCNTs at an AC signal of 140 kV_{pp} m⁻¹, 15 kHz, and laser power of 20 mW. **c** The captured MWCNTs can be translated to a new spot on the surface of the electrode but **d**, **f** lose their vertical orientation and are released from the aggregation once the AC signal and laser spot are deactivated. **g** A single unmanipulated, unaligned and **h** vertically aligned MWCNT after the application of the electric field of 140 kV_{pp} m⁻¹ and 55 kHz and laser power of 20 mW. **i** Once trapped, the MWCNT can be translated across the electrode surface. **j** MWCNT was released after the AC signal and laser spot are turned off. Reproduced with permission of Springer Nature

Though REP allows for the dynamic manipulation of MWCNTs, it was also possible to permanent pattern them to the electrode surface by simultaneously applying an AC field of $200 \text{ kV}_{pp} \text{ m}^{-1}$ and DC offset of $12 \text{ kV} \text{ m}^{-1}$. Experimental observations indicated that the density of the captured MWCNT can be increased by decreasing the AC frequency from 75 to 15 kHz or increasing the solution concentration from 7.8×10^7 to 2.3×10^8 CNTs mL⁻¹.

4.2 Particle Translation

The conventional experimental setup for REP was implemented to translate and rotate particle geometries.⁷⁹ The authors show (Figs. 1c, 8a–c) how a particle aggregation of over 600 particles is moved to new spot on the electrode substrate. In this example, the illumination source is deactivated and activated at a short distance away. Initially, the particles scatter and then accumulate in the new spot 40 μ m away in under 6 s.

Translation of colloidal aggregation is also possible by combining REP with a scanning nearinfrared (NIR) laser system (Fig. 8d–g).⁷⁴ The optical experimental components and setup are detailed in Velasco et al.⁷⁴ publication. The REP chip in this system consisted of a top electrode plate sputtered with chrome/gold and a bottom ITO coated coverslip. 1.0 µm polystyrene particles were dispersed in aqueous potassium chloride. In this study, particle accumulation was observed at AC signal of 40 kHz at 3.6 V_{rms}, 36 mW laser output power, and scanning periods between 25 ms and 66.7 s. Particle aggregation behavior was affected by the unsteady electrothermal hydrodynamics caused by the scanning laser. Four behavior cases were examined (Fig. 8d-g), the first being a static spot where compact colloidal assemblies are usually observed due to large fluid drag which dominate over dipole-dipole repulsive forces (Fig. 8d).^{32, 81} A second case consisted of the translation of the colloidal group (Fig. 5e). This case is observed when the electrothermal fluid velocity exceeds the velocity of the laser. When the speed of the scanning laser is close to or higher than the electrothermal fluid velocity, colloids can be translated with the moving laser but because of dipole-dipole repulsive forces and weaker hydrodynamic drag attractive forces, particles are quickly released (Fig. 8f, g). The study



Figure 8: Examples of particle aggregations translated with REP platforms. **a**-**c** Polystyrene particle (690 nm) assembly with over 600 particles were moved when the laser spot was turned off and activated at a spot 40 μ m away with an AC signal of 2.0 V_{pp} at 1.6 kHz, an illumination intensity of 20 mW, and the conventional optical setup. Reproduced with permission of the Royal Society of Chemistry. Particles were also translated with a scanning laser system, images show particle assembly behavior during a **d** static the laser spot, as well as, laser scan period of **e** 66.7 s, **f** 6.7 s, and **g** 67 ms. Copyright Wiley–VCH Verlag GmbH & Co. KGaA. Reproduced with permission **f**.

showed that to achieve steadier colloidal aggregations, the laser should be programmed to shorter scanning periods. The oscillatory nature of electrothermal fluid dynamics in the scanning REP system could be useful in hydrodynamic drag sorting and micromixing applications.

4.2.1 Translating Bacteria

Similar to the translation of spherical particles, bacteria aggregation was moved to different spot on the electrode surface by repositioning the stage. Bacteria were observed to remain in the vertical orientation and move at the same velocity of the translation of the stage. It was also observed that the alignment of cells is critical for capture, as non-oriented cells have the ability swim and overcome the electrothermal fluid flow.

4.3 Particle Sorting

Particle sorting is also possible through REP (Figs. 1e, f, 9).^{33, 81} The frequency dependent behavior of colloidal assemblies in REP makes it possible to sort and characterize particles due to their AC electrokinetic behavior. The

critical frequency (Fig. 3b) at which particles are no longer trapped is due to the relaxation polarization of the particle's electric double layer according to Schwarz's fundamental model⁶³, where particles alike have a critical frequency that is inversely proportional to the particle diameter.

Like previous experimental configurations mentioned above, a parallel ITO electrode chip was used in combination with a near infrared holographic system.⁸¹ 100, 20, and 3 µL of a 2% solids of 2, 1, and 0.5 µm (respectively) carboxylate-modified polystyrene particles (Invitrogen, OR, USA) were suspended in 2.0 mL of potassium chloride solution with a measured conductivity of 2.4 mS m⁻¹. In this study, particles were sorted by size as a result of the frequencydependent polarization of particles' ionic double laver, where the relaxation frequency is inversely proportional to particle surface area (a^2) .³² All three particles sizes were trapped at AC signal of 38 kHz, 13.4 V_{pp}, and 23 mW (Fig. 9a). Frequency signal was increased to 80 kHz causing the 2.0 µm particles to be discharged leaving the 0.5 and 1 µm particle trapped (Fig. 9b). At a frequency of 106 kHz, the 1 µm particles were released



Figure 9: Demonstrations of particle sorting based on **a**–**d** size and **e**–**f** type. **a** All particles (2, 1, and 0.5 μ m) were captured 38 kHz, 13.4 V_{pp}, and 23 mW. **b** Increasing frequency to 80 kHz, caused 2 μ m to be discharged into the medium, leaving the trapped 1 and 0.5 μ m on the electrode surface. **c** At 106 kHz, only 0.5 μ m particles remained aggregated. 1 μ m polystyrene and silica (non-florescent) were sorted showing REP can characterize particle type. **d** At 150 kHz, 19.8 V_{pp}, and laser power of 23 mW only polystyrene particles were aggregated. **e** At a lower frequency of 90 kHz, both polystyrene and silica particles were captured. Reproduced with permission from IOP publishing

(Fig. 9c). The authors plotted and portrayed a second-order polynomial relationship between the trapping frequency and particle diameter, as well as, AC potential^{32, 81}, determining that with increasing particle diameter, the critical frequency decreases (Fig. 9c).

Size-based particle sorting was also achieved using the thin film REP chips.⁷³ In these chips, 1.0 and 2.0 μ m particle were trapped at 1.6 V_{DC}, 10 V_{pp}, and 50 kHz. When the AC frequency was increased to 100 kHz, 2.0 μ m particles were released.

An alternate way of size-based particle sorting with REP is executed by isolating the larger particle group from a rigid cluster of smaller diameter particles.⁷⁸ In this scenario, smaller particles (compared to larger particles) have reduced dipole–dipole repulsive forces and at their minimum inter-particle distance become a rigid particle cluster that resists REP translation. As an example, 0.5 and 1.0 μ m polystyrene particles were initially captured at 130 kHz, 25 V_{pp}, and 20 mW. At 50 kHz, the spacing between 0.5 μ m particles reached its minimum causing the small diameter particle cluster to become rigid, but leaving the 1.0 μ m particle group with ability to move to another location (Fig. S2).

Additionally, the sorting of unlike particles was demonstrated with 1 μ m silica and polystyrene particles (Fig. 9d, e).⁸¹ In these experiments, polystyrene particles were captured at 23 mW, 150 kHz, and 19.8 V_{pp}. As the frequency was decreased, silica particles were observed to aggregate at 90–130 kHz. Particle type sorting was observed with a solution conductivity of 2.4 and 4.1 mS m⁻¹. Hence, particle sorting based on particle polarizability, perhaps even surface chemistry (i.e., altered EDL polarizability), is possible.

4.3.1 Sorting Bacteria

In Kwon et al. study, REP was used to separate bacteria taking advantage of the critical frequency of particles emerging from their surface charge density (Fig. 10).³³ For cells with similar surface charges, the critical frequency is assumed as the inverse of particle diameter squared. REP sizebased separation was performed on similar zetapotential S. cerevisiae (~ 5 µm in diameter) and S. aureus (~1 µm in diameter) (Fig. 8f-h). Initially, both bacteria were aggregated on the surface at 10.07 V_{pp} , 17.5 kHz, and 20 mW. Increasing frequency to 38.9 kHz caused the larger S. cerevisiae to be released with a few of S. aureus. Though, authors did not perform viability test, the bacteria was assumed to be unaffected by REP as they remained at the bottom surface and were never visualized floating within the microchannel.

5 Conclusions

Rapid electrokinetic patterning is a technique which combines the advantages of AC electrokinetics and optical energy. The multiphysical nature of this technique offers challenges in developing a comprehensive theoretical model for REP, though significant strides have been made to describe the governing physical mechanisms.

The various capabilities and potentials of REP make it a versatile technique to be applied in a variety of colloidal concentration applications, including creating artificial architectures such as photonic crystals. The frequency-dependent polarization of the particles' or cells' electric double layer can be explored, complementing other electrokinetic techniques like dielectrophoresis that explore interfacial polarization behavior. Rapid aggregation and patterning of colloids is one of the pivotal advantages of REP because it





enables the development of not only high sensitivity biochemical sensors but also high-performance LOC systems.

Introducing more complex microelectrode structures (ex: interdigitated electrodes) will enable the study of the simultaneous effects of REP and non-uniform electrokinetics like DEP, leading to a new chapter of fundamental and applied research in interface and colloidal science. The REP platform could be modified further with an alternative illumination source. Therefore, the laser used to induce the nonuniform temperature distribution in a conventional REP experiment can be replaced with more low-cost, compact illumination tools like light-emitting diodes, paving the path to development of more portable low-cost microfluidic devices. Inexpensive REP systems with alternative illumination sources and novel electrode materials will extend its range of applications. Constructing a broad illumination REP system creates an inexpensive method of massive parallel particle manipulation and particle assembly that can allow various shape patterning and colloidal aggregations.

REP can be applied to variety of existing lab-on-a-chip techniques such as particle concentration, creation of artificial architectures, microfluidic mixing, and/or pumping. The dynamic control of laser illumination can induce electrothermal flow anywhere on the chip, enabling enhanced, on-demand and reconfigurable microfluidic mixing or pumping. REP's ability to sort, characterize electrokinetic particle behavior, and enhance particle detection will advance many lab-on-a-chip sensing processes because stabilization is essential for accurate diagnostic analysis. The added ability to translate massive particle groups will improve bead-based assays by bringing biologically modified particles into contact with surfaces of interest.

Electronic supplementary material

Below is the link to the electronic supplementary material.Supplementary material 1 (DOCX 3954 kb)

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